

3 **Johannes von Kries's Conception of Probability, its**  
4 **Roots, and Modern Developments: Introduction**5 **Jacob Rosenthal<sup>1</sup> · Carsten Seck<sup>2</sup>**6  
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9 The papers in this special section originate from a two-day conference on “Johannes von  
10 Kries's conception of probability, its roots and impact”, held in September 2012 in Bonn.  
11 Johannes von Kries (1853–1928) was a renowned physiologist and professor at Freiburg,  
12 who also worked on the methodology and foundations of science. In 1886, he published his  
13 “Die Principien der Wahrscheinlichkeitsrechnung. Eine logische Untersuchung” (The  
14 Principles of the Probability Calculus. A Logical Investigation). This book had consider-  
15 able influence at its time and was re-issued unaltered in 1927. In 1916, von Kries concisely  
16 described his core ideas on probability also in a comprehensive work called “Logik.  
17 Grundzüge einer kritischen und formalen Urteilslehre” (Logic. Outlines of a Critical and  
18 Formal Theory of Judgment). In the “Principien”, von Kries is less concerned with the  
19 calculus of probability—there are almost no formulas contained in the book—than with the  
20 meaning and background of ascriptions of numerical probability. In modern terms, his  
21 issue was with the truth conditions of such statements. Von Kries suspected that precise  
22 numerical statements of probability are without proper foundation in many fields, and he  
23 set out to clarify the circumstances in which they are meaningful. He rejects probabilities  
24 as subjective degrees of confidence (“psychologism”), the classical, Laplacean account  
25 (“logical interpretation”) as well as the relative frequency theory (“empirical interpreta-  
26 tion”) of probability. He then puts forward, carefully explicates and explores an original  
27 proposal, which explains the importance of the book.

28 Von Kries's core notion is that of a measurable “Spielraum” (range, leeway), and his  
29 “Spielraumtheorie” or range conception of probability is the first to use a fundamental idea

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30 in the interpretation of probabilities that came to be known later in a somewhat different  
31 guise as the “method of arbitrary functions”. Von Kries locates the truth conditions of  
32 probability statements in the generating conditions of the phenomena to which the calculus  
33 of probability can be successfully applied. He identifies these, roughly speaking, as phe-  
34 nomena with generating conditions such that all attachments of continuous probability  
35 distributions to these yield the same outcome probabilities for the events of interest. In its  
36 core applications, the approach presupposes a classical mechanical setting with instability  
37 (similar initial states may lead to different outcomes), and in addition, that an event of  
38 interest is represented with constant proportion all over the state space. The same basic  
39 idea was later put forward and developed in different ways by several other writers. Today,  
40 the best known of them may be Henri Poincaré. While von Kries’s treatment lacks  
41 mathematical rigour, he had a genuine grasp of the origin of probabilistic phenomena in  
42 deterministic settings. He was the first to take such an approach to probabilities and their  
43 interpretation, but the exact nature of the von Kriesian probabilities is not easy to deter-  
44 mine. He strongly influenced logicians like John Maynard Keynes as well as frequentists  
45 like Hans Reichenbach.

46 Nowadays, views on probability that share central features with von Kries’s account are,  
47 e.g., taken by Marshall Abrams, Jacob Rosenthal, and notably Michael Strevens. They may  
48 be said to constitute a third way on objective probability, besides frequentist and propensity  
49 accounts. (We take David Lewis’s best-system analysis of probabilistic laws of nature and  
50 objective chance to be a sophisticated version of frequentism. If this means stretching the  
51 label “frequentism” too far, we have to reckon with still another way on objective  
52 probability.) Although it never became mainstream, the basic idea of the “third way” is  
53 ever-recurring and can be explicated in various ways with non-trivial differences. Many of  
54 its versions were developed independently of von Kries, but he may nevertheless be called  
55 the originator of the whole approach, and so his particular account deserves attention. As  
56 indicated, von Kries is difficult to understand in certain places. In particular, it is not fully  
57 clear whether he proposes an objective interpretation of probability in the current sense, or  
58 whether his account is rather meant to be epistemic (or, as he might have said, “logical”)  
59 in kind. This corresponds to the fact that “arbitrary functions” on a state space can be  
60 understood in several ways, e.g., as representing empirical distributions of relative fre-  
61 quencies, or as reflecting our ignorance with regard to the obtaining particular initial state.  
62 Outcome probabilities that may be called “objective” result either way, but in the latter  
63 case, these “objective” probabilities are nothing but resilient subjective or epistemic ones.  
64 It may, however, be a mistake to force our distinction between subjective (or epistemic)  
65 and objective (or ontic) probabilities upon von Kries.

66 The papers collected in this special section address historical as well as systematic  
67 issues connected to the “Spielraumtheorie” or range conception of probability. We use this  
68 von Kriesian label as an umbrella term for the third way on objective probability, although  
69 there are considerable differences between von Kries’s original account and, say, Poin-  
70 caré’s “method of arbitrary functions”, Michael Strevens’s “microconstant probability” or  
71 Marshall Abrams’s “mechanistic probability”. The overarching term is justified in view of  
72 the shared basic idea and analogous problems. Helmut Pulte’s paper investigates the  
73 background of the “Spielraumtheorie”. He puts the von Kriesian ideas in their historical  
74 setting and explores the underlying philosophical and scientific views of von Kries. From  
75 there, he addresses certain problems of and tensions within von Kries’s original account.  
76 The interpretation of this account is the focus of Sandy Zabell’s paper. He carefully  
77 explores von Kries’s central notions as well as the relation to and impact on several of his  
78 contemporaries, with a view to “principles of insufficient reason” in particular. Jacob



79 Rosenthal puts forward and discusses a modernized version of von Kries's account,  
80 relating it to current alternatives. John Roberts addresses a basic problem that besets the  
81 whole third way on objective probability, namely, the status of the "input probabilities" or  
82 "arbitrary functions" the approach seems to presuppose: what their meaning is, and how to  
83 justify the required smoothness condition. Claus Beisbart fruitfully contrasts the range  
84 conception to the currently most influential account of objective probability: David  
85 Lewis's best-system approach. Last but not least, Bernd Buldt provides a comprehensive  
86 and detailed bio-bibliography of Johannes von Kries.

87 While the papers of Buldt, Pulte and Zabell share a historical focus on von Kries and his  
88 contemporaries, Beisbart and Roberts refer to variants of the approach that are in vogue  
89 today and discuss it in a systematic way. Rosenthal's paper is somewhat in between and  
90 provides a link between von Kries and modern writers. On the whole, the papers offer a  
91 historical as well as systematic account of the range conception as the third way on  
92 objective probability. We would very much like to thank the DFG for funding the con-  
93 ference, the Journal for General Philosophy of Science for publishing this special issue, and  
94 above all the speakers and contributors for their papers and many exciting and in-depth  
95 discussions.  
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