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When cardinality determines the power set

We investigate when the predicate " $x = \text{Powerset}(y)$ " can be $\Sigma_1(\text{Card})$ where Card is a predicate for the cardinal numbers. This has relations to the H\"artig quantifier logic which is intermediate between first and second order logic. We discuss L\"owenheim-Skolem numbers for such a logic, and, to an extent, analyse the class of its validities. (This is joint work with Jouko V\"a\"an\"anen.)